

**VIT**

Institute of Technology

DEPARTMENT  
SCHOOL OF A  
Winter 5  
Continuous Assess

MATHEMATICS  
ADVANCED SCIENCES  
Winter 2022-23  
Test - I, March 2023

Course Code : BMAT102L  
Course Name : Differential Equations  
Duration : 90 minutes

Date of Exam: 27.03.2023  
Slot : B2+TB2+TBB2  
Max. Marks : 50

## Answer All the Questions

Q. No	Question	Marks
1	Solve the differential equation $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = x^2 - 3x$ by the method of undetermined coefficients.	10M
2	Solve the differential equation $x^2\frac{d^2y}{dx^2} - 4x\frac{dy}{dx} + 6y = x^2$ by the method of variation of parameters.	10M
3	If a voltage of $100 \cos 10t$ V is impressed on a circuit containing elements with resistance $40 \Omega$ , inductor $1$ H and capacitance $16 \times 10^{-4}$ F in series, then find the charge at time $t$ in the circuit.	10M
4	i) Form a partial differential equation by eliminating the arbitrary functions from the relation $z = f\left(\frac{xy}{z}\right)$ .	5M
	ii) Find the complete solution of the partial differential equation $z^2 = 1 + p^2 + q^2$ , where $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$ .	5M
5	Find the general solution of the partial differential equation $\left(\frac{b-c}{a}\right)yzp + \left(\frac{c-a}{b}\right)xzq = \left(\frac{a-b}{c}\right)xy$ , where $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$ .	10M