



### Final Assessment Test - April 2025

Course: BMAT102L - Differential Equations and Transforms

Class NBR(s): 1048 / 1049 / 1051 / 1052 / 1053 / 1054 /  
1055 / 1056 / 1057 / 1058 / 1059 / 1060 / 1061 / 1062 /  
1063 / 1064 / 1065 / 1066 / 1067 / 1068 / 1069 / 1070 /  
3640

Slot: C1+TC1+TCC1

Time: Three Hours

Max. Marks: 100

- KEEPING MOBILE PHONE/ANY ELECTRONIC GADGETS, EVEN IN 'OFF' POSITION IS TREATED AS EXAM MALPRACTICE
- DON'T WRITE ANYTHING ON THE QUESTION PAPER

Answer ALL Questions  
(10 X 10 = 100 Marks)

1. Solve  $t^2 \frac{d^2x}{dt^2} + 9x = \log t$  by the method of variation of parameters. [10]
  2. Use the method of undetermined coefficients, to solve the differential equation [10]  
$$\frac{d^2y}{dx^2} - 4 \frac{dy}{dx} + 4y = e^{2x} + \cos 2x.$$
  3. (i) Obtain the partial differential equation by eliminating the arbitrary function [5]  
from  $\phi(x^2 + y^2 + z^2, z^2 - 2xy) = 0$ .  
(ii) Solve  $q^2 = z^2 p^2 (1 - p^2)$ , where  $p = \frac{\partial z}{\partial x}, q = \frac{\partial z}{\partial y}$ . [5]
  4. Solve  $4 \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 3u, u(0, y) = 3e^{-y} - e^{-5y}$  using the method of separation of [10]  
variables.
  5. (i) Evaluate the improper integral  $\int_0^{\infty} \frac{\cos 2t - \cos 3t}{t} dt$  using Laplace transform. [10]  
(ii) Find the Laplace transform of a periodic function  $f(t) = \begin{cases} 1, & 0 < t < 1 \\ t, & 1 < t < 2 \end{cases}$   
with period 2.
  6. Using the Convolution theorem, find  $L^{-1} \left[ \frac{s}{s^4 + 37s^2 + 36} \right]$ . [10]
  - 7.a) Solve the following differential equation using Laplace transform. [10]  
$$\frac{d^2x}{dt^2} + 4x = H(t - \pi) + H(t - 2\pi), x(0) = 0 = x'(0).$$
- OR
- 7.b) Obtain the solution of  $u_x + u_t + u = 0$  with [10]  
 $u(0, t) = 0 (t > 0), u(x, 0) = \cot x (x > 0)$  using Laplace Transform.

8.a) Find the Fourier series for the function  $f(x) = x \sin x$ ,  $0 < x < 2\pi$ . [10]

OR

8.b) Find the half range Fourier cosine series of  $f(x) = x(2-x)$  in  $0 \leq x \leq 3$ , and [10]  
hence find the sum  $\frac{1}{1^2} - \frac{3}{2^2} + \frac{1}{3^2} - \frac{3}{4^2} + \dots$

9. Find the sine transform of  $f(x) = \frac{e^{-3x}}{x}$ . [10]

10. Find the response of the system  $x_{n+2} - 8x_{n+1} + 15x_n = 1$ , with  $x_0 = 0, x_1 = 0$  [10]  
using Z-transform.

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