



Final Assessment Test April 2019

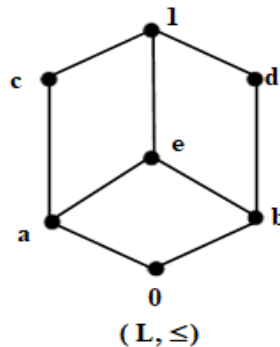
Course: **MAT1014 - Discrete Mathematics and Graph Theory**
 Class NBR(s): **0668 / 0670 / 0671 / 0675 / 0678 / 0680 / 0683 / 0684 / 0687 / 0692 / 0711 / 0713 / 0715 / 3334**
 Time: **Three Hours**

Slot: **A1+TA1+TAA1+V1**
 Max. Marks: **100**

Answer any FIVE Questions
(5 X 20 = 100 Marks)

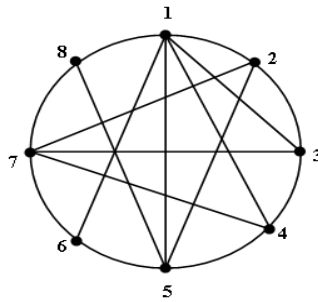


1. a) Obtain the PCNF and PDNF of $S: (\neg P \rightarrow R) \wedge (Q \leftrightarrow P)$. Also determine a unique representation for the PCNF and PDNF of S . Is S a tautology? [10]
 b) Show that R is a valid conclusion from the premises $P \rightarrow Q$, $Q \rightarrow R$, $\neg(P \wedge R)$, $P \vee R$. [10]
2. a) Verify the validity of the following argument. [10]
 'Every living thing is a plant or an animal. John's gold fish is alive and it is not a plant. All animals have hearts. Therefore John's gold fish has a heart.'
 b) Show that $(\forall x) (P(x) \vee Q(x)) \Rightarrow (\forall x) P(x) \vee (\exists x) Q(x)$ using indirect method of proof. [10]
3. a) State and prove Lagrange's theorem for finite groups. [10]
 b) Let $G = \{1, -1, i, -i\}$. [10]
 i. Is G is a group under usual multiplication?
 ii. Is G abelian?
 iii. Is G cyclic?
 iv. What is the order of every element in G ?
4. a) Let S be any set, and $\rho(S)$ its power set. Verify if $(\rho(S), \leq)$ is a partially ordered relation, where $\leq$ denotes the relation 'is a subset of'. Draw the Hasse diagram of $(\rho(S), \leq)$, when $X = \{1, 2, 3, 4\}$. [10]
 b) Given the Hasse diagram $(L, \leq)$, verify if it is modular, distributive and complemented. Justify your answer. [10]

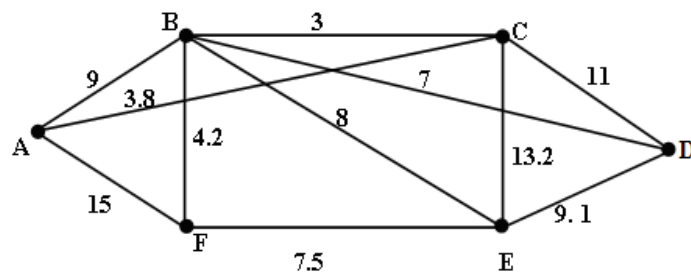


5. a) Verify if the following Boolean polynomials P and Q are equivalent. If so determine their sum of product canonical form. [10]
 $P(x, y, z) = (x \oplus y) * (x' \oplus z) * (y \oplus z)$.
 $Q(x, y, z) = (x \oplus y) * (x' \oplus z)$.
 b) Minimize the following expression using Quine-McCluskey's method [10]
 $wxyz + \overline{w}x\overline{y}z + \overline{w}x\overline{y}z + \overline{w}x\overline{y}z + \overline{w}x\overline{y}z$.

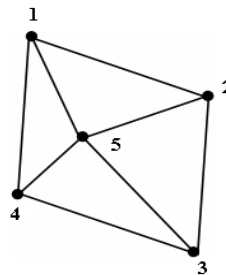
6. a) State and prove a necessary and sufficient condition for a connected graph G to be Euler. **[10]**
 b) State Kuratowski's theorem on graph planarity. Hence verify if the following graph is planar using Kuratowski's theorem. **[10]**



7. a) Determine a minimum weighted spanning tree for the following graph G using Prim's and Kruskal's algorithm. **[10]**



- b) Given the following graph G , determine **[10]**



- The chromatic number of G .
- A chromatic partition of G .
- The chromatic polynomial for G .

