

**VIT**

Vellore Institute of Technology

School of Electronics Engineering

Winter Sem 2023-2024

Continuous Assessment Test - I

BECE313L – Information Theory and Coding

Marks: 50

B.Tech (ECE)

SLOT: A1

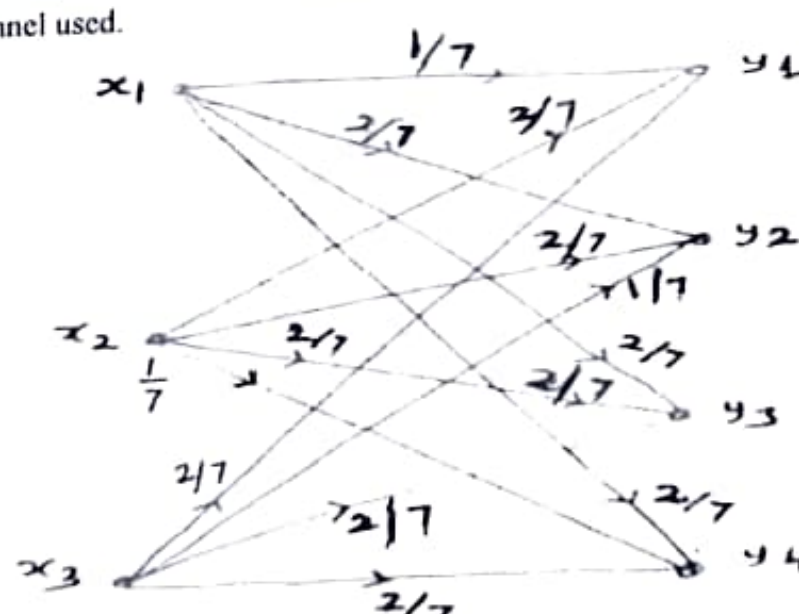
Q. No	Answer All Questions	Marks	CO	BL																				
1	a) Verify the rule of additivity for the following symbols $S = \{A, B, C, D\}$ and their corresponding probabilities are $P = \{1/8, 1/8, 1/4, 1/2\}$ b) A binary source generates symbols $\{0, 1\}$ and their corresponding probabilities are $\{0.25, 0.75\}$. The binary source is extended in such a way to generate second order extension. Calculate the entropy of extended source and also verify the extension property.	6	CO1	L2																				
2	A transmitter transmits 5 symbols X_1, X_2, X_3, X_4, X_5 and the receiver receives 4 symbols Y_1, Y_2, Y_3, Y_4. The joint probability matrix for the communication is given below in Figure 1. Determine $H(X)$, $H(Y)$, $H(X, Y)$, $H(X/Y)$ and $H(Y/X)$. <table border="1"> <tr> <td>0.25</td><td>0</td><td>0</td><td>0</td></tr> <tr> <td>0.1</td><td>0.3</td><td>0</td><td>0</td></tr> <tr> <td>0</td><td>0.05</td><td>0.10</td><td>0</td></tr> <tr> <td>0</td><td>0</td><td>0.05</td><td>0.1</td></tr> <tr> <td>0</td><td>0</td><td>0.05</td><td>0</td></tr> </table>	0.25	0	0	0	0.1	0.3	0	0	0	0.05	0.10	0	0	0	0.05	0.1	0	0	0.05	0	4 5.3, 1.77	CO1	L2
0.25	0	0	0																					
0.1	0.3	0	0																					
0	0.05	0.10	0																					
0	0	0.05	0.1																					
0	0	0.05	0																					
3	A discrete memory less source emits messages $\{x_1, x_2, x_3\}$. The source is connected to the receiver as shown in Figure 2. Find the capacity of the channel used. 	10	CO2	L2																				

Figure 1

Figure 2

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A BSC has the following noise matrix with source probabilities $P(x_1) = 1/2$ & $P(x_2) = 1/2$. The noise matrix $P(y_j/x_i)$ is given below in Figure 3.

$$\begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

Figure 3

Determine all entropies, channel capacity and channel efficiency.

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The following output has been generated by a discrete memoryless source in 1 minute duration.

a e d a e c c a c b a a b c b a d b a f

Apply Shannon-Fano Coding techniques with coded alphabets $\{0, 1, 2\}$ and calculate the efficiency of the code generated.

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C

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