



# VIT<sup>®</sup>

Vellore Institute of Technology  
(Deemed to be University under section 3 of UGC Act, 1956)

Vellore – 632014, Tamil Nadu, India

## SCHOOL OF MECHANICAL ENGINEERING WINTER SEMESTER 2023-2024

### CONTINUOUS ASSESSMENT TEST – I

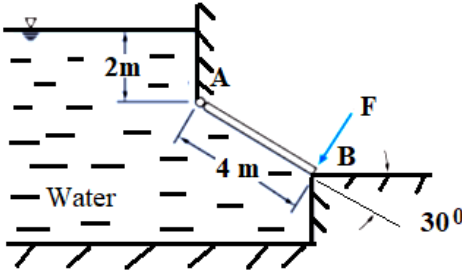
Programme Name & Branch : B.Tech- Automotive, Mechanical, Manufacturing Engineering  
 Course Code and Name : BMEE204L and Fluid Mechanics and Machines  
 Slot : E2+TE2  
 Class Number(s) : VL2023240504623, VL2023240504557, VL2023240504624, VL2023240504564  
 Faculty Members : Dr. Rajesh Kanna, Dr. Sreethul Das,  
 Dr. Mohamed Ibrahim M, Dr. Sreeja Sadasivan  
 Date and Time of Exam : 15-02-2024, 2.00 PM-3.30 PM  
 Duration : 90 minutes Max. Marks: 5 x 10 M=50M

**General instruction(s): 1. Assume suitable data, if required,**

**Answer ALL the Questions**

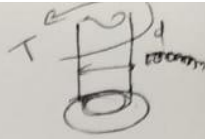
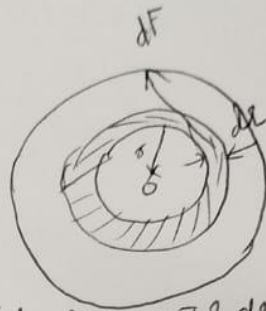
Q. No	Question	Marks	Course Outcome (CO)	Bloom's Taxonomy (BL)
1.	The shaft rests on a 2.5-mm-thin film of oil having a viscosity of $0.068 \text{ N s / m}^2$ . If the shaft is rotating at a constant angular velocity of $\omega = 2.2 \text{ rad/s}$ , determine the torque <b>T</b> that must be applied to the shaft to maintain the motion at i) $r = 80 \text{ mm}$ and ii) $r = 40 \text{ mm}$ . Assume the velocity profile within the oil is linear.	10	1	3
2.	The system in Fig. 1 is open to 1 atm on the right side. (a) If $L = 118 \text{ cm}$ , what is the air pressure in container A? (b) Conversely, if $P = 128 \text{ kPa}$ , what is the length $L$ ?	10	1	3
<p>Fig.1</p>				
3.	When a hydrometer having a stem diameter of $7.62 \text{ mm}$ is placed in water, the stem protrudes $80 \text{ mm}$ above the water surface. If the water is replaced with a liquid having a specific gravity of $1.1$ , how much of the stem would protrude above the liquid surface? The hydrometer weighs $0.187 \text{ N}$ .	10	1	4

Vellore – 632014, Tamil Nadu, India  
**SCHOOL OF MECHANICAL ENGINEERING**  
**WINTER SEMESTER 2023-2024**

4.	<p>The gate AB shown is hinged at A. The gate is 4.2 m wide normal to the plane of the diagram. Calculate the force required at B to hold the gate closed.</p>  <p style="text-align: center;">Fig. 2</p>	10	1	4
5.	<p>A steady, incompressible, two-dimensional velocity field is given by the following components in the <math>xy</math>-plane:</p> $u = 1.1 + 2.8x + 0.65y; \quad v = 0.98 - 2.1x - 2.8y$ <p>Calculate the acceleration field (<math>a_x</math> and <math>a_y</math>) and calculate the acceleration at the point <math>(x, y) = (-2, 3)</math>.</p>	10	2	3

$$\tau = \mu \frac{du}{dy}$$

$$u = r\omega$$



The shear force that oil exerts on the differential area  $2\pi r dr = dA$

$$dF = \tau \times dA = \mu \frac{du}{dy} \times 2\pi r dr$$

Since the velocity distribution is linear, velocity gradient is constant  $\frac{du}{dy} = \frac{u}{t}$

$$\int dT = \mu \frac{u}{t} \times 2\pi \int r^2 dy$$

Put  $u = r\omega$

$$T = \frac{\mu \omega}{t} 2\pi \int_0^R r^3 dy = \frac{2\pi \mu \omega R^4}{t \cdot 4}$$

$$T = \frac{\pi \mu \omega R^4}{2t}$$

at  $r = 80\text{mm}$

$$T_1 = \frac{\pi \times 0.068 \times 2.2 \times (0.08)^4}{2 \times 2.5 \times 10^{-3}} = 3.85 \times 10^{-3} \text{ Nm}$$

at  $r = 40\text{mm}$

$$T_2 = 2.406 \times 10^{-4} \text{ Nm}$$

$$2) P_A + \rho_{Hg} g (0.31 - 0.15) - \rho_w g (L \sin 55 - 0.18) = P_{atm}$$

$$P_A - 136 \times 9810 \times 0.16 - 9810 (L \sin 55 - 0.18) = 101325$$

$$P_A - 8035.8 L = 120,90576$$

$$\text{If } L = 118 \text{ cm} \quad P_A = \underline{\underline{130.38 \text{ kPa}}}$$

$$\text{If } P_A = 128 \text{ kPa} \quad L = \underline{\underline{0.882 \text{ m}}}$$

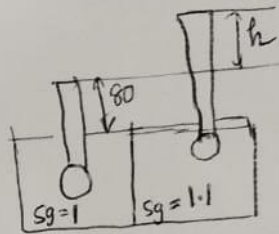
3) when hydrometer is placed in liquid of  $S_g = 1.1$

$$W = F_B$$

$$0.187 \text{ N} = (\rho g)_{\text{liquid}} \times V_1$$

$$0.187 = 1.1 \times 9810 \times V_1$$

$$V_1 = \underline{\underline{1.7329 \times 10^{-5}}}$$



when the hydrometer is placed water

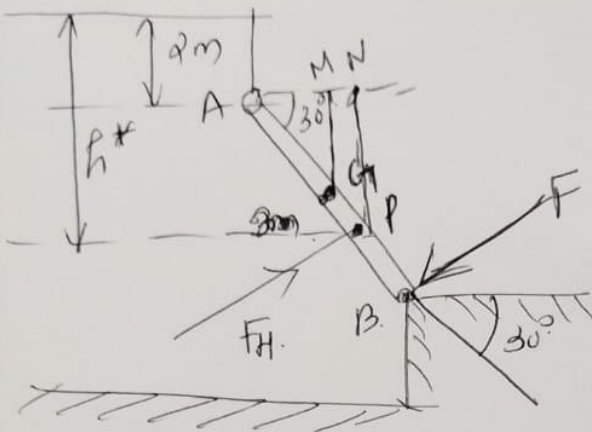
$$0.187 = (\rho g)_{\text{water}} \left[ V_1 + \frac{\pi}{4} d^2 h \right]$$

$$h = 38 \text{ mm}$$

The stem would protrude above  $\underline{\underline{38 \text{ mm} + 80 \text{ mm} = 118 \text{ mm}}}$  above the liquid surface.

$$5) a_n = -9.233 \text{ m/sec}^2$$

$$a_y = 14.371 \text{ m/sec}^2$$



$$\Rightarrow F_h = \rho g A \bar{h}$$

$$F_h = 9810 \times (4 \times 4.2) \times 3$$

$$F_h = \underline{\underline{494.424 \text{ kN}}}$$

$$\Rightarrow \bar{h}^* = \bar{h} + \frac{I_{AG}}{A \bar{h}} \sin^2 \alpha$$

$$\bar{h}^* = \frac{3 + \frac{22.4}{(4 \times 4.2) \times 3} \sin^2 30}{}$$

$$\bar{h}^* = \underline{\underline{3.11 \text{ m}}}$$

$$\Rightarrow \sum M_A = 0$$

$$F_h \times AP = F \times BA$$

$$494.24 \times 10^3 \times 2.22 = F \times 4$$

$$F = \underline{\underline{274.303 \text{ kN}}}$$

$\Delta AMG$

$$\sin 30 = \frac{MG}{AG}$$

$$AG = 2 \text{ m}$$

$$MG = 1 \text{ m}$$

$$\bar{h}^* = MG + 2 \text{ m} = \underline{\underline{3 \text{ m}}}$$

$$I_{AG} = \frac{4.2 \times 4^3}{12} = \underline{\underline{22.4 \text{ m}^4}}$$

$\Delta APN$

$$NP = \bar{h}^* - 2 = \underline{\underline{1.11 \text{ m}}}$$

$$\sin 30 = \frac{NP}{AP} = \frac{1.11}{AP}$$

$$AP = \underline{\underline{2.22 \text{ m}}}$$