



VIT[®]

Vellore Institute of Technology
(Deemed to be University under section 3 of UGC Act, 1956)

Continuous Assessment Test (CAT - I), February 2024			
Programme	: B. Tech	Semester	: Winter 2023-2024
Course Title	: Engineering Physics	Course Code	: BPHY101L
School	: School of Advanced Sciences	Slot	: D2+TD2
Duration	: 90 mins	Max. Marks	: 50
Class No	: 1914, 1906, 1910, 1912, 1916, 1903, 1905, 1915, 1913, 1911, 1908		

Part – A (5 x 10 = 50)

Answer ALL Questions

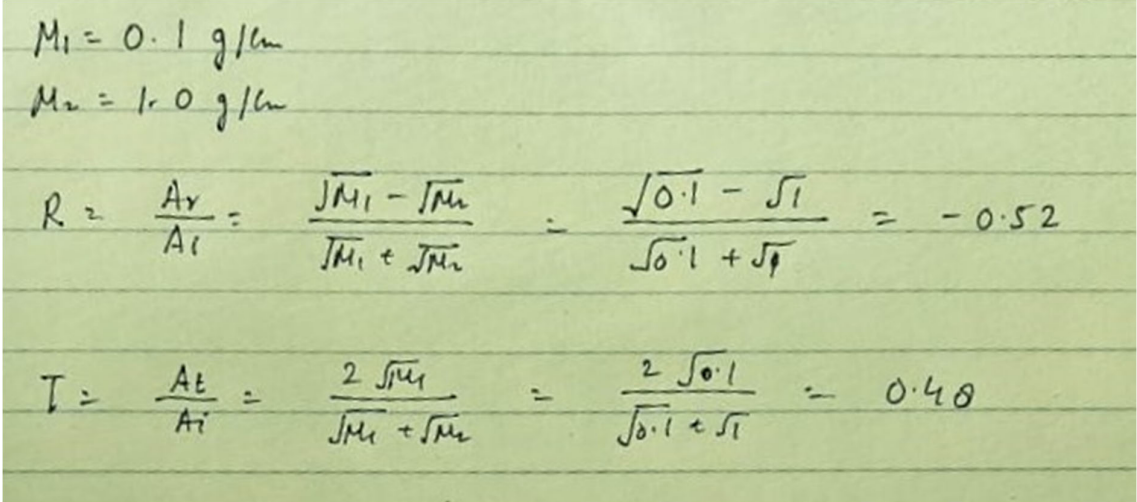
Sl. No	Questions	Max Marks
1	What is a transverse wave? Explain with an example. With a clear diagram and assumptions, derive the equation for the wave propagating on a string of linear mass density μ and under a tension T.	10
2	Derive the expression for displacement, wavelength, and frequency of n^{th} mode of a standing wave on a string of length L fixed at two ends. Draw the wave patterns for the second and fifth harmonics.	10
3	(a) What is the characteristic impedance of a string? With suitable diagrams, discuss what happens when a wave on a string is reflected by a (i) free end and (ii) fixed end. (b) A wave travels through a junction between two strings of different linear mass densities. The linear mass density of the first medium is 0.1 gcm^{-1} and that of the second medium is 1 gcm^{-1} . Compute the reflection and transmission coefficients of the wave.	5 5
4	Starting from the differential form of Maxwell's equations, derive the wave equations for electric and magnetic fields in free space. Further, detail how Maxwell concluded that the light must be an electromagnetic wave.	10
5	(a) Consider the vector field $\vec{F} = xe^y \hat{i} + ye^z \hat{j} + ze^x \hat{k}$. Compute the <i>curl</i> and the <i>divergence of curl</i> of the vector field, showing all the intermediate steps. (b) Explain the construction and working of the Hertz experiment.	5 5



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Answer Key

Sl. No	Questions	Max Marks
1	Definition of transverse wave and example 2 marks <u>Derivation of wave equation</u> Labelled diagram 2 marks Assumptions 2 marks Derivation 4 marks	10
2	Derivation of displacement of standing wave 4 marks Eigenfrequency and wavelength expression: 4 marks Standing wave pattern for second and fifth harmonic: 2 marks	10
3	(a) Definition of characteristic impedance 1 mark (i) discussion of wave reflection at a free end (with diagram) 2 marks (ii) discussion of wave reflection at a fixed end (with diagram) 2 marks (b) Formulae for reflection (R) and transmission (T) coefficients 2 marks Calculation and results 3 marks	5
	 <p> $M_1 = 0.1 \text{ g/cm}$ $M_2 = 1.0 \text{ g/cm}$ $R = \frac{A_r}{A_i} = \frac{\sqrt{M_1} - \sqrt{M_2}}{\sqrt{M_1} + \sqrt{M_2}} = \frac{\sqrt{0.1} - \sqrt{1}}{\sqrt{0.1} + \sqrt{1}} = -0.52$ $T = \frac{A_t}{A_i} = \frac{2\sqrt{M_1}}{\sqrt{M_1} + \sqrt{M_2}} = \frac{2\sqrt{0.1}}{\sqrt{0.1} + \sqrt{1}} = 0.48$ </p>	5
	Reflection coefficient = -0.52 Transmission coefficient = 0.48	

4	Maxwell's equations in free space Wave equation derivation for electric field Wave equation derivation for magnetic field EM wave speed calculation and comparing it with the speed of light	2 marks 3 marks 3 marks 2 marks	10
5	(a) Compute the curl of the vector field (show all the steps) Compute the divergence of curl of the vector field (show all the steps)	3 marks 2 marks	5
<p> $\vec{F} = xe^y \hat{i} + ye^z \hat{j} + ze^x \hat{k}$ $\nabla \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ xe^y & ye^z & ze^x \end{vmatrix}$ $= \hat{i} (0 - ye^z) - \hat{j} (ze^x - 0) + \hat{k} (0 - xe^y)$ $= -ye^z \hat{i} - ze^x \hat{j} - xe^y \hat{k}$ $\nabla \cdot (\nabla \times \vec{F}) = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \cdot (-ye^z \hat{i} - ze^x \hat{j} - xe^y \hat{k})$ $= -\frac{\partial}{\partial x} (ye^z) - \frac{\partial}{\partial y} (ze^x) - \frac{\partial}{\partial z} (xe^y)$ $= -0 - 0 - 0$ $= 0$ </p>			
(b) Hertz experiment – components Hertz experiment – working		2.5 marks 2.5 marks	